

Total Marks: 50

Time: 2 Hrs.

1. Answer any two questions: $10 * 2 = 20$

- a) Explain how the slope of MR curve depends on the curvature of AR curve.
- b) Utility function of a consumer is $U = e^{x_1 x_2}$. Budget constraint is $y_0 = p_1 x_1 + p_2 x_2$. Find the expression for price elasticity of demand for both x_1 and x_2 .
- c) Solve by matrix inversion method

$$\begin{aligned} X+2y-z &= -9 \\ 2x-y+3z &= -2 \\ 3x+2y+3z &= 9 \end{aligned}$$

- d) i) Let the utility function $U = x^2 y^3$. Determine the expenditure function. 7
- ii) Suppose the demand function is given by $p = 8 - 3q$ and cost function is $c = 3 + 2q$. Find out the profit maximizing output, price and maximum amount of profit. 3

2. Answer any four questions: $5 * 4 = 20$

- a) Derive the series of the function $\log(1+x)$ by using the Maclaurin Series.
- b) A production function is $q = 7K^{0.5} L^{0.3}$. If prices of K and L are Rs. 2 and Rs. 3 respectively, obtain the equation of expansion path.
- c) Derive compensated demand function of the given utility function $U = q_1, q_2$ and the budget constraint $p_1 q_1 + p_2 q_2 = M$.

d) Given $u = \begin{bmatrix} 5 \\ 1 \end{bmatrix}$ & $v = \begin{bmatrix} 0 \\ 3 \end{bmatrix}$ find the following graphically

- i) $2v$,
- ii) $u+v$
- iii) $v-u$
- iv) $2u+3v$
- v) $4u-2v$

e) Find the rank of the given matrix

$$A = \begin{bmatrix} 1 & 1 & 1 \\ 1 & -1 & 0 \\ 1 & 1 & 1 \end{bmatrix}$$

f) a. Consider the following household demand function:

$$q^d = q^d(p, y) = 10y^2 + 2y^4 p^{-2} - 3p^3 \quad (p, y > 0)$$